



# Hilbert-Huang Transform:

A method for analyzing nonlinear  
and nonstationary data

presented by:

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**N A S A   M e d i c a l   T e c h n o l o g y   S u m m i t**

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# Presentation Outline

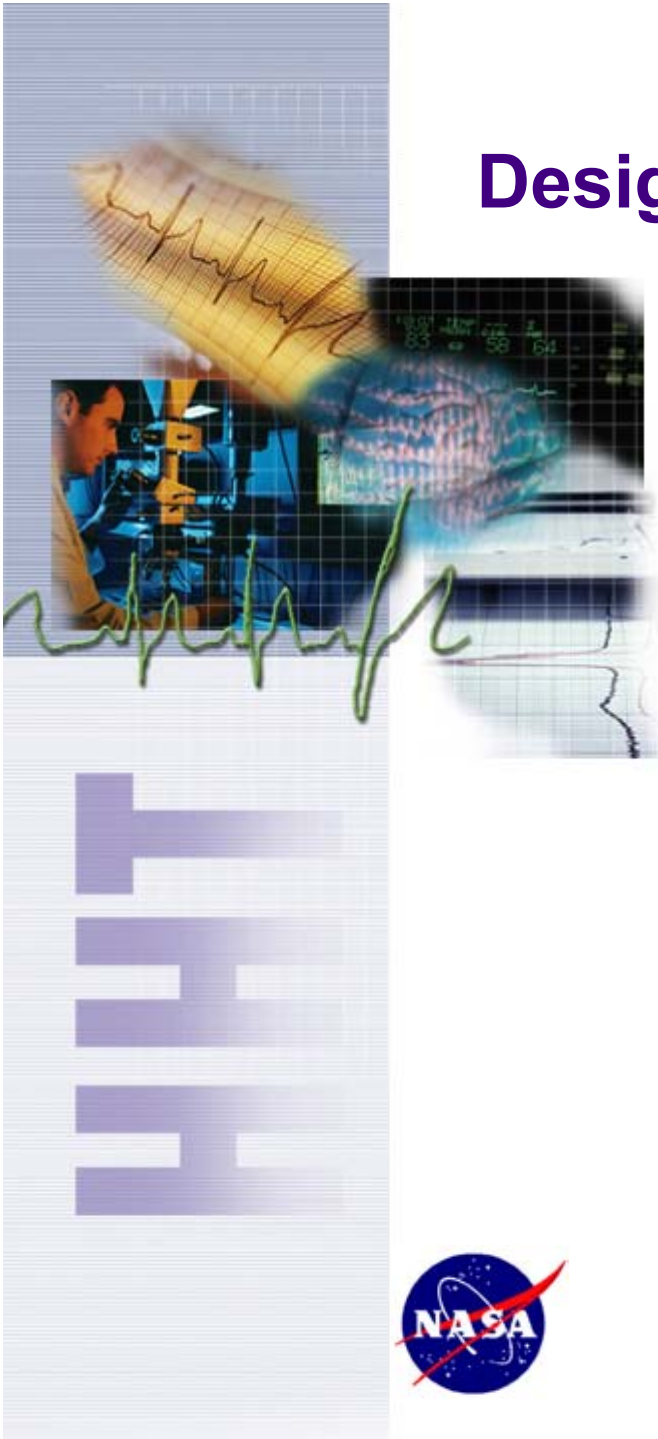
- Design motivation and concept inception
- Technology description
- Market potential
- Status of development
- Technology details and results
- Summary
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- Acknowledgements
- Q&A



# Design Motivation & Concept Inception

**Problems result from characteristics of data:**

- **Insufficient sample size**
- **Nonstationary data**
- **Nonlinear data**



# Design Motivation & Concept Inception

## Prior art:

- Wavelet analysis, Wigner-Ville transforms, Fourier analysis
- Singular spectral analysis, nonlinear phase plane analysis

**Each has limitations**

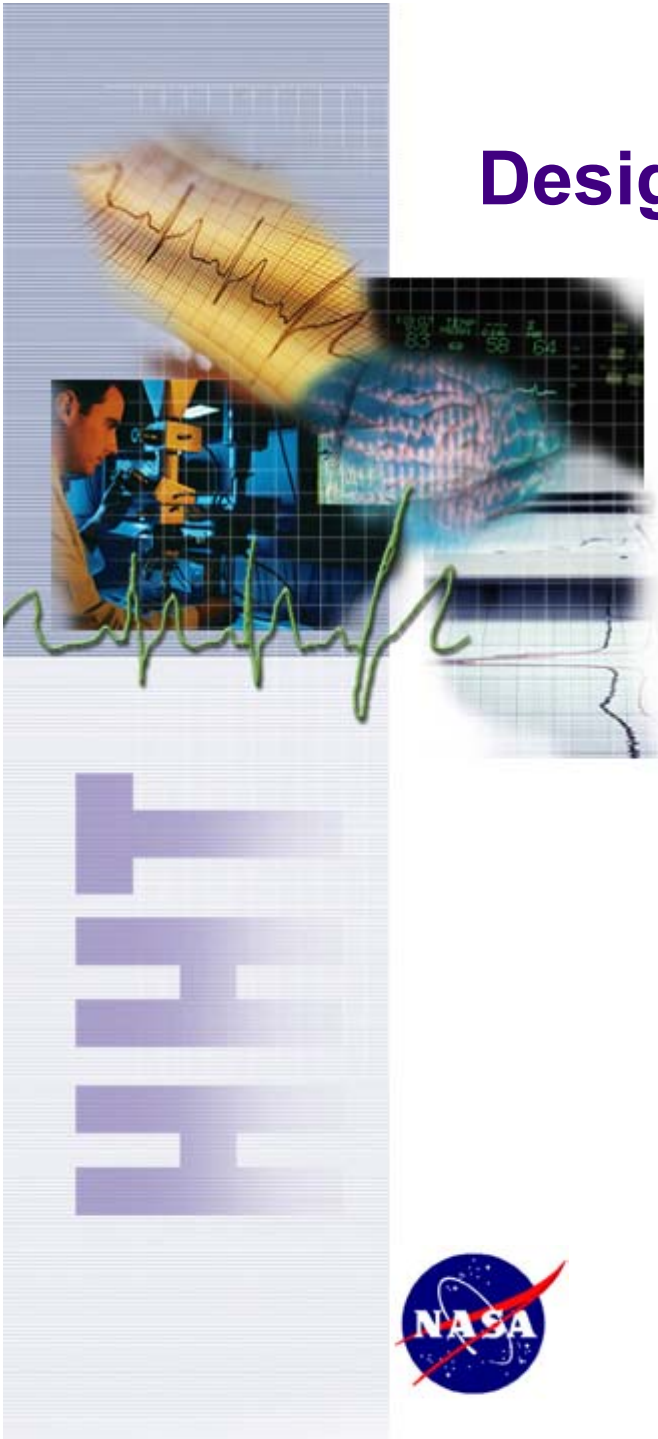
**Result is inaccurate interpretation  
of underlying physics**



# Design Motivation & Concept Inception

## The basic problem in analyzing data:

- All existing methods are for either *linear* or *stationary* data or they assume *deterministic processes*.
- Most actual data are *nonlinear*, *nonstationary*, and *stochastic*.

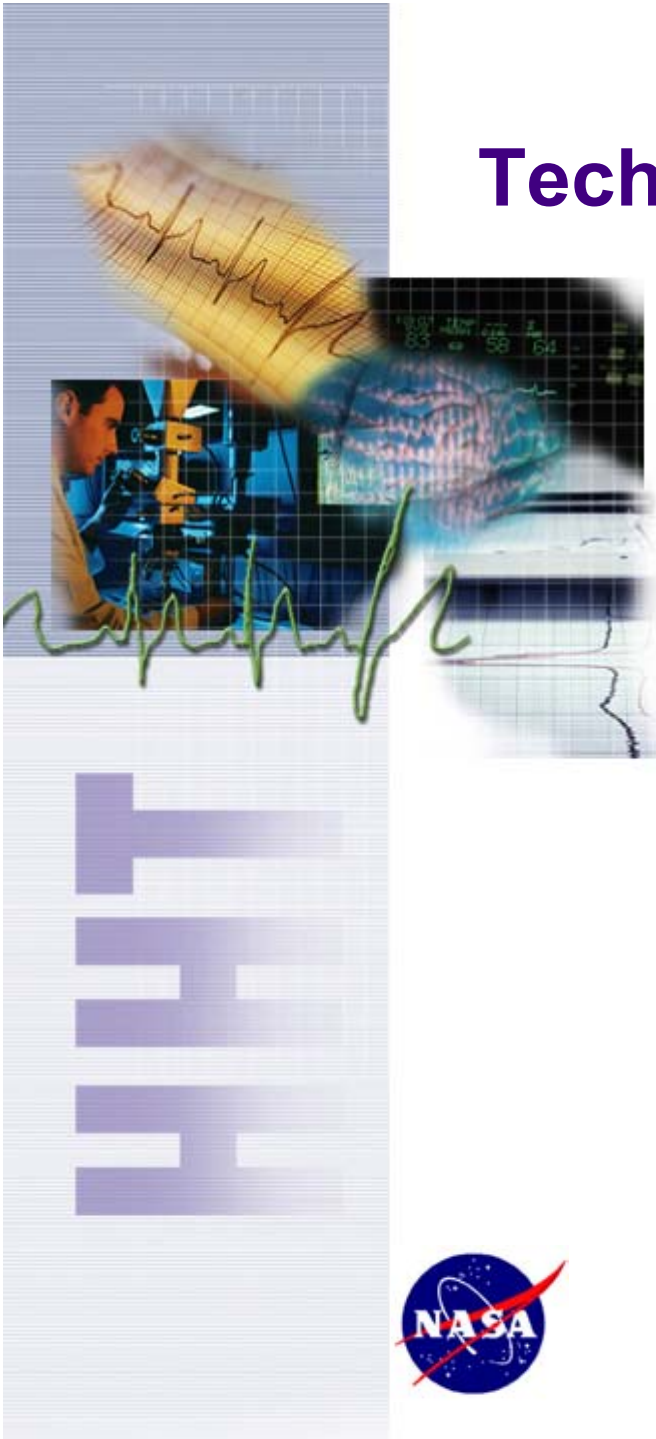




# Technology Description

## Goal:

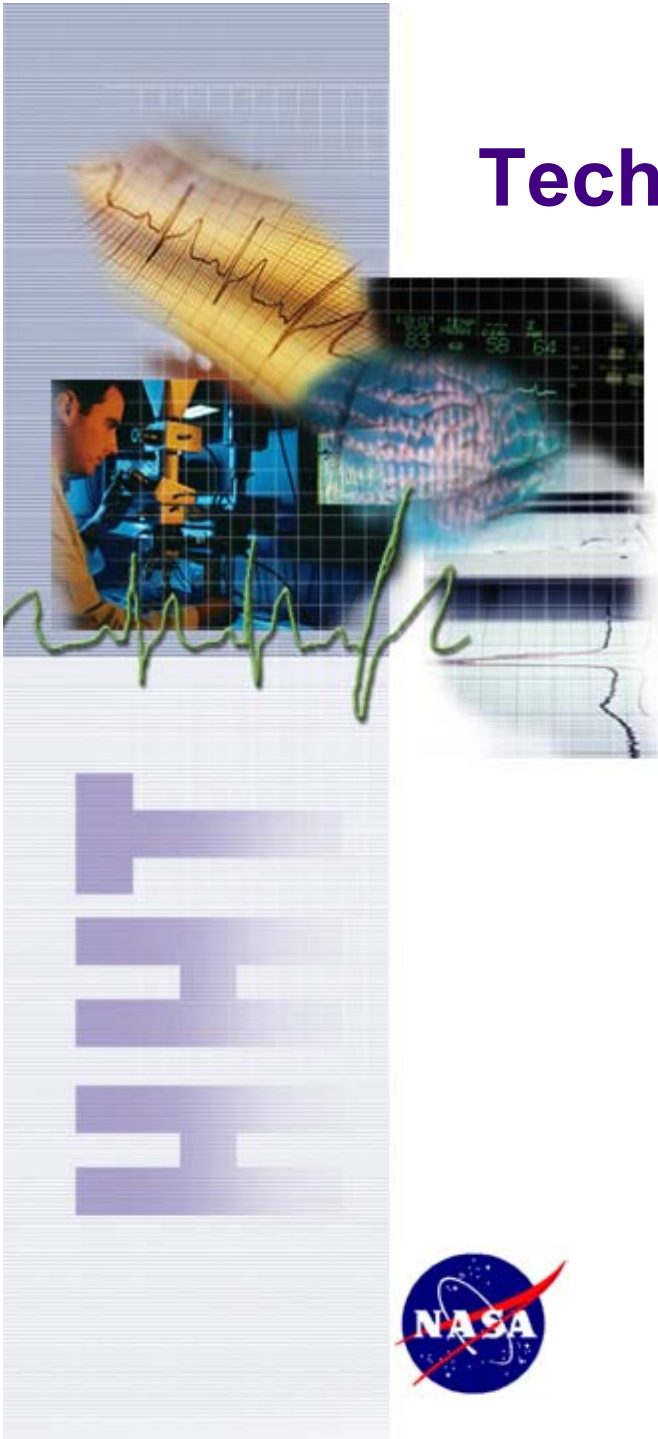
- Develop a means of accurately analyzing nonlinear, nonstationary data



# Technology Description

## Basic concept:

- Any applied mathematics method that analyzes nonlinear, nonstationary data has to be adaptive.
- To be effective and rich in information, any basis has to involve a finite and often small number of discrete *modes* that retain the intrinsic properties of the original data.



# Technology Description

## Technical goals of data analysis:

- To define local time scale or frequency
- To define local energy density
- To define joint frequency-energy distribution





# Technology Description

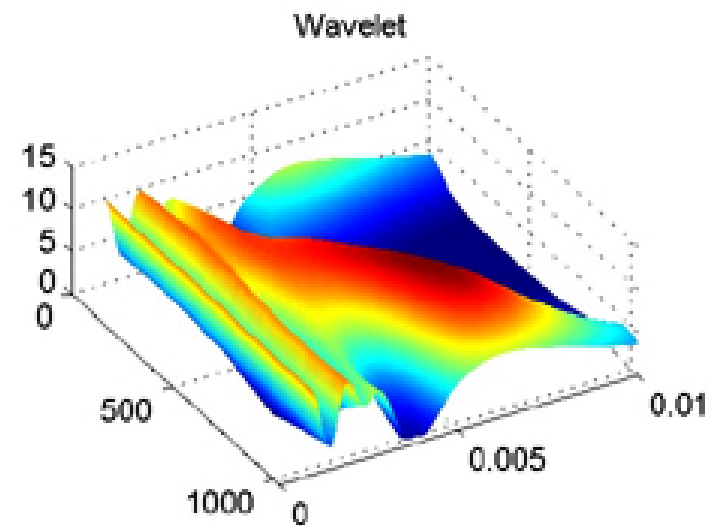
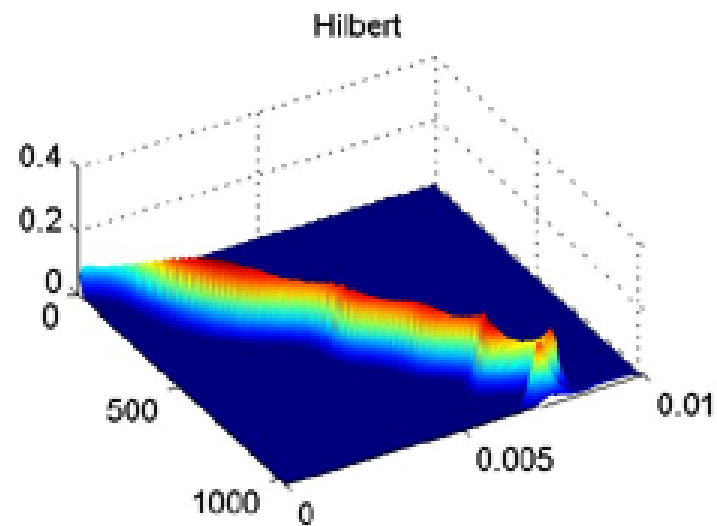
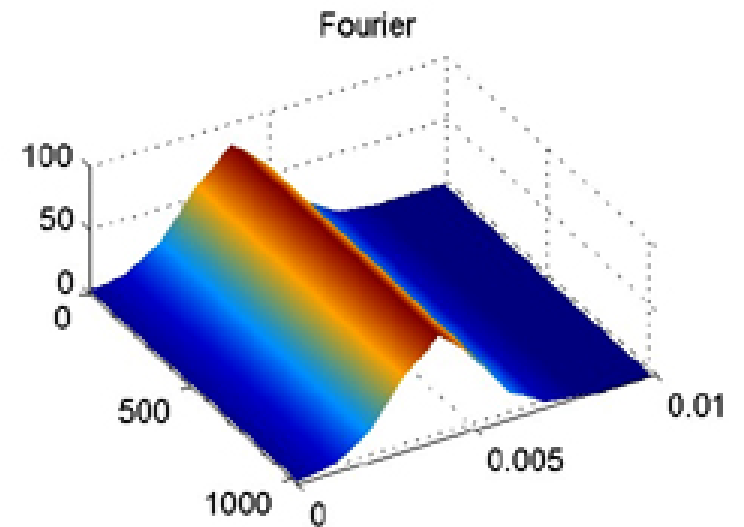
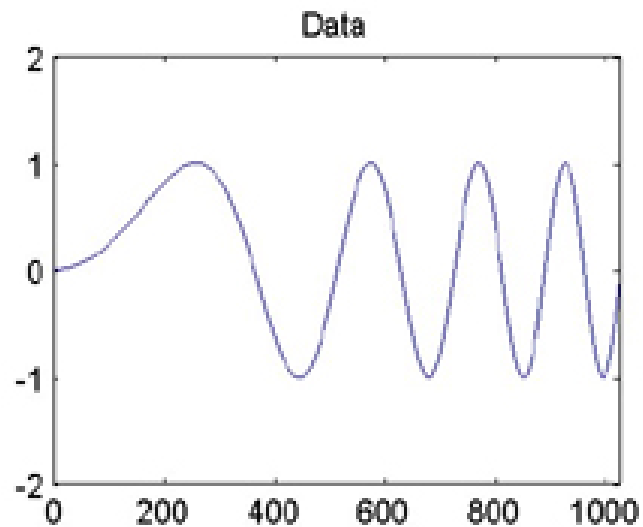
## Method:

- Empirical Mode Decomposition method extracts intrinsic mode functions (IMFs), (i.e., oscillation modes within data) which still retain intrinsic characteristics of the data
- Hilbert-Huang Transform (HHT) converts IMFs into local energy and instantaneous frequencies as a base for the full energy-frequency-time distribution of data (i.e., Hilbert spectrum)
- Physical signal is filtered by reconstructing signal from selected IMFs or IMF sections



## Technology Description

# Comparisons: Fourier, Hilbert & Wavelet



# Technology Description

## Results:

- An adaptive basis to filter signal
- Frequency defined as a function of time by differentiation rather than convolution analysis
- Sharp identification of embedded structures
- A more simple and revealing interpretation than prior methods



Market Potential

# Key Considerations

- Conceptually simple and direct
- An efficient, adaptive, user-friendly set of algorithms
- Capable of analyzing nonlinear and nonstationary signals as well as linear and stationary signals



Market Potential

## Key Considerations

- Improves accuracy by using an adaptive basis to preserve intrinsic properties of data
- Yields results with more physical meaning and a different perspective than existing tools
- Useful in analyzing a variety of physiological signals as well as many other signals from nonlinear and nonstationary processes





## Market Potential

# Benefits

### Precision:

- More precise time-frequency representation of signal data than with “Fourier-type” methods
- Sharper filter performance than provided by “Fourier-type” methods



## Market Potential

# Benefits

### Flexibility:

- Designed for processing nonlinear and nonstationary signals
- Flexible enough to analyze any data (linear or nonlinear) and stationary or nonstationary signals



## Market Potential

# Benefits

### Accuracy:

- Preserves intrinsic properties of data
- Offers a microscopic view of data not limited by the uncertainty principle
- Does not impose *a priori* assumptions on data, as in Fourier methods (i.e., that assume linear and stationary data)



## Market Potential

# Benefits

### Easy implementation:

- Easy and inexpensive to implement in software or hardware

### Real-time operation:

- Operates and yields physically meaningful results in real time



## Market Potential

# Benefits

### Multifunctionality:

- Generates IMFs through an adaptive algorithm from a data set with which other methods fail
- Examines previously unattainable results for aiding diagnosis
- Provides new, quantitative measurements that enhance understanding of underlying physiological phenomena





## Market Potential **Applications**



### **NASA:**

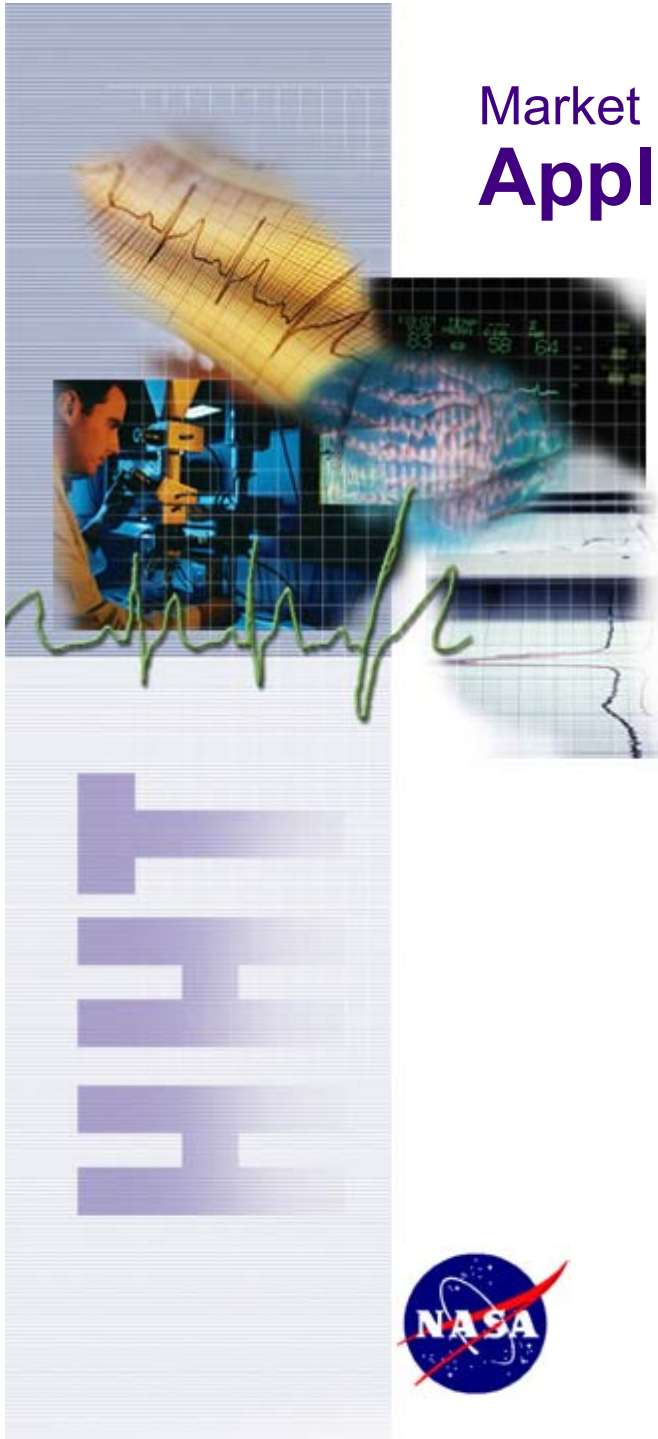
- Analyzing and correcting satellite data
- Analyzing data to understand underlying phenomena
- Fusing data from multi-sensors

### **Other government entities:**

- **DOT** (seismic load and nondestructive testing)
- **FBI** (speech analysis and speaker identification)
- **U.S. Navy** (shock loading and nondestructive testing)
- **NIST** (machine health monitoring)



# Market Potential **Applications**



## **Commercial:**

- Predicting incipient failure of machinery
- Analyzing sound waves, electromagnetic waves, heat conduction/convection, and mechanical vibrations
- Interpreting nonstationary signals

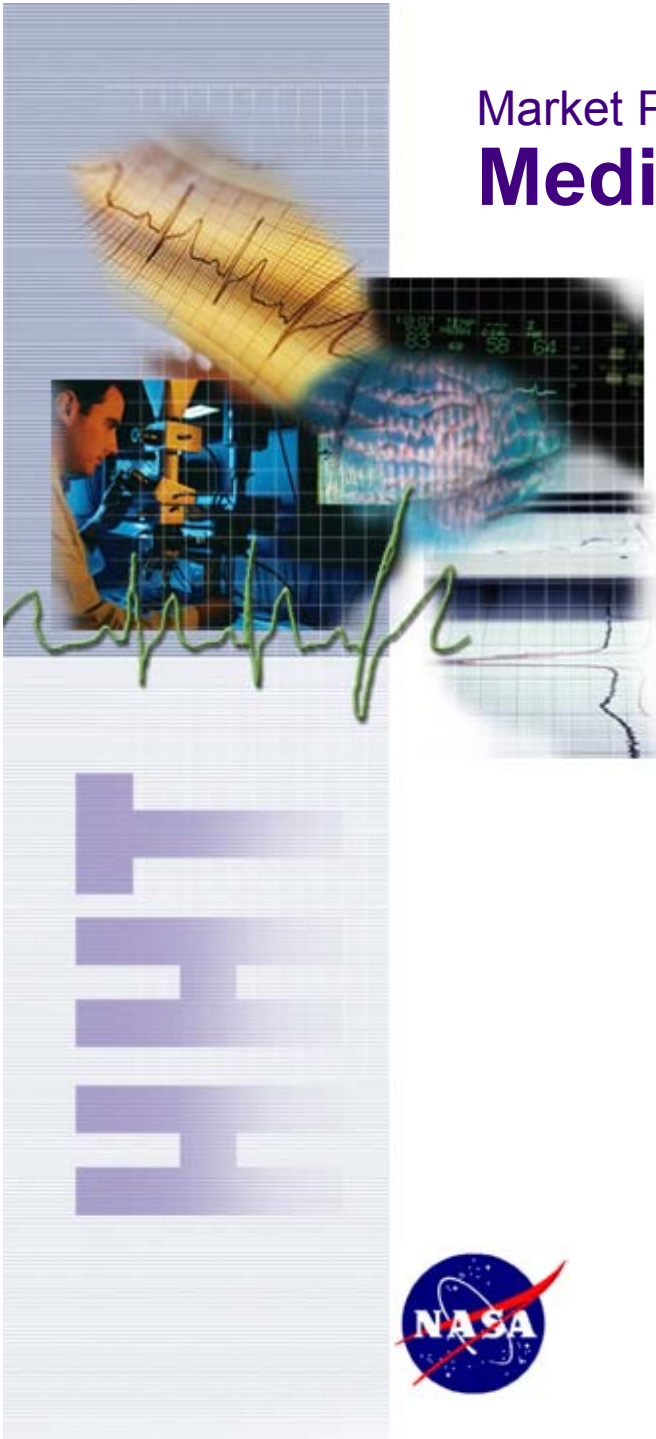
## **Medical**

Market Potential

## Medical Applications

### Analysis of acoustic, biological, and physiological signals:

- Blood pressure
- Heart pulse interval
- Heart rate
- Plethysmogram signals
- Electroencephalogram (EEG) signals
- Temperature signals
- Blood oxygen levels
- Speech (i.e., soundwaves)
- Electrocardiogram (ECG)



Market Potential

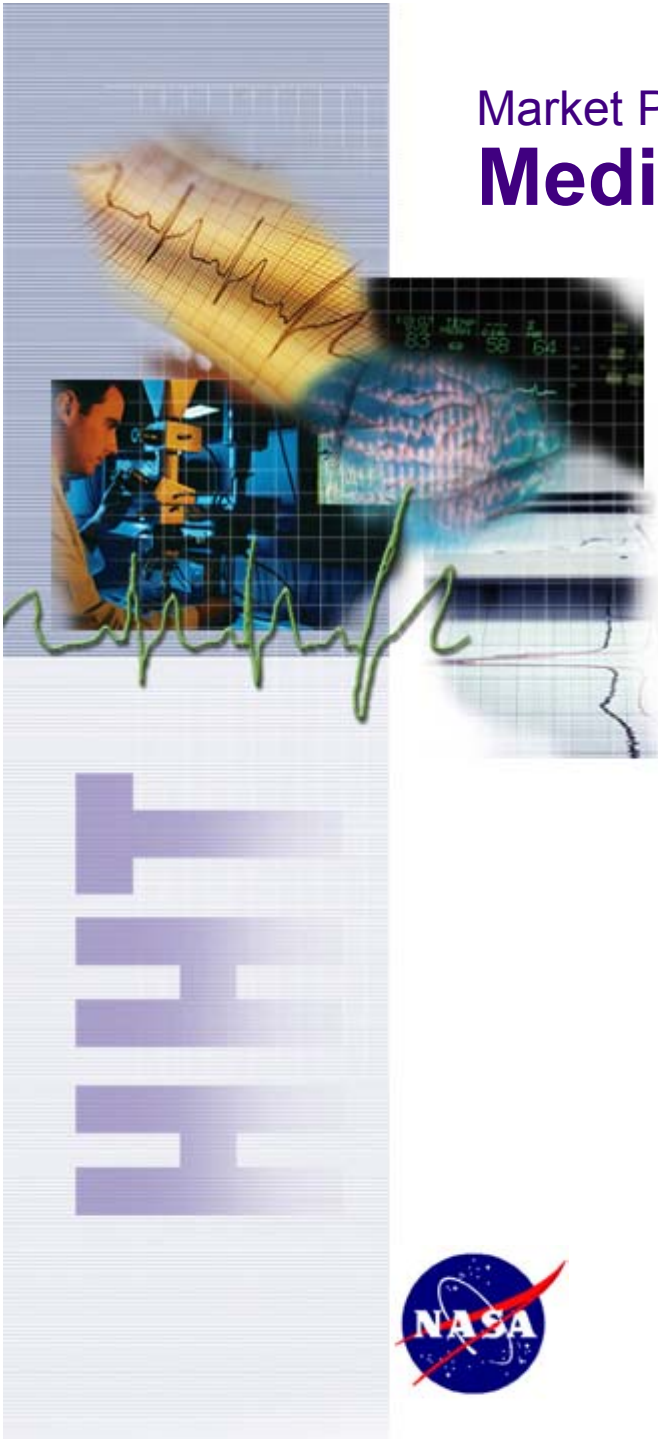
# Medical Applications

## Noise filtering:

- Reducing noise
- Increasing signal clarity

## Research:

- Studying the effect of one variable on another to get a deeper understanding of the underlying physiological phenomenon



Market Potential

## Medical Applications

### Diagnosis of an abnormal condition or disease:

- Sleep apnea
- Neurological disorders (e.g., epilepsy and Parkinson's disease)

### *In vitro* studies:

- Current flow across membranes (i.e., patch clamping)
- Fluorescence in confocal microscopy
- Analysis of spectroscopic signals





Market Potential

# Medical Applications

## Identification of outliers:

- Heart rate
- Blood pressure
- Other physiological functions

Deriving an analytical function  
representative of a biological  
phenomenon



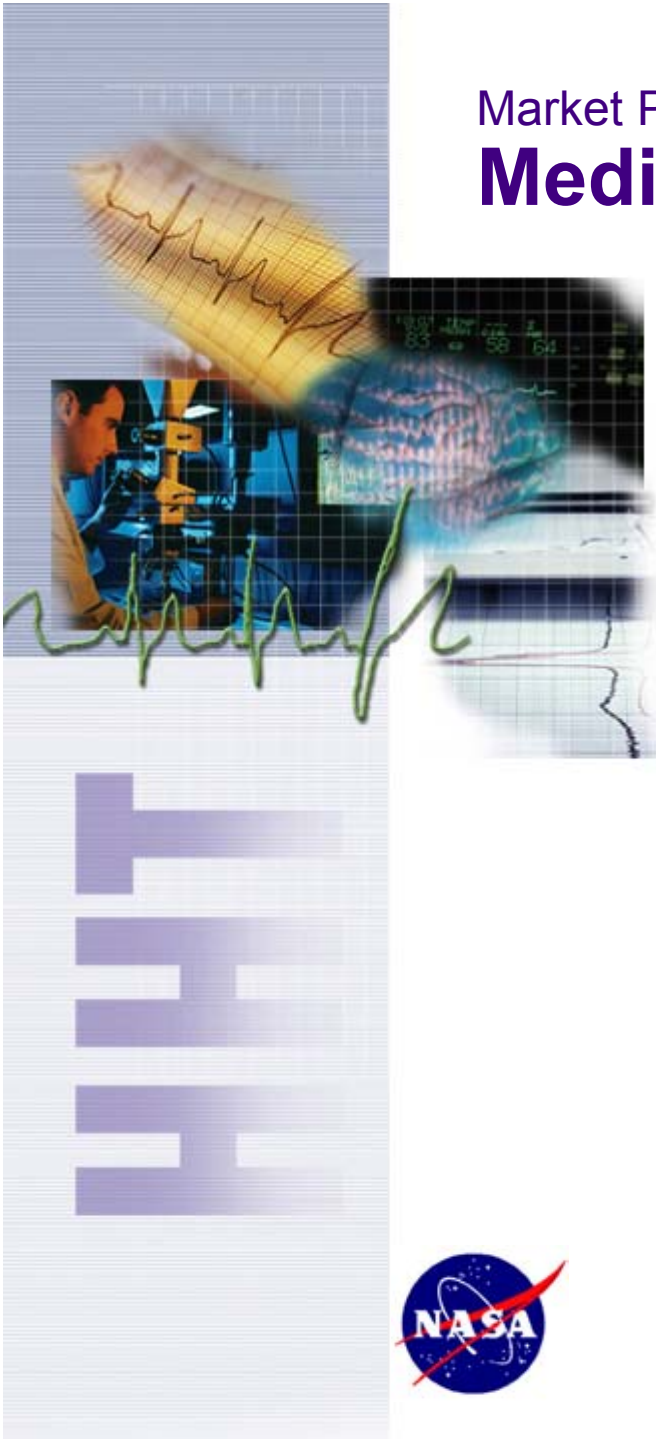
Market Potential

# Medical Applications

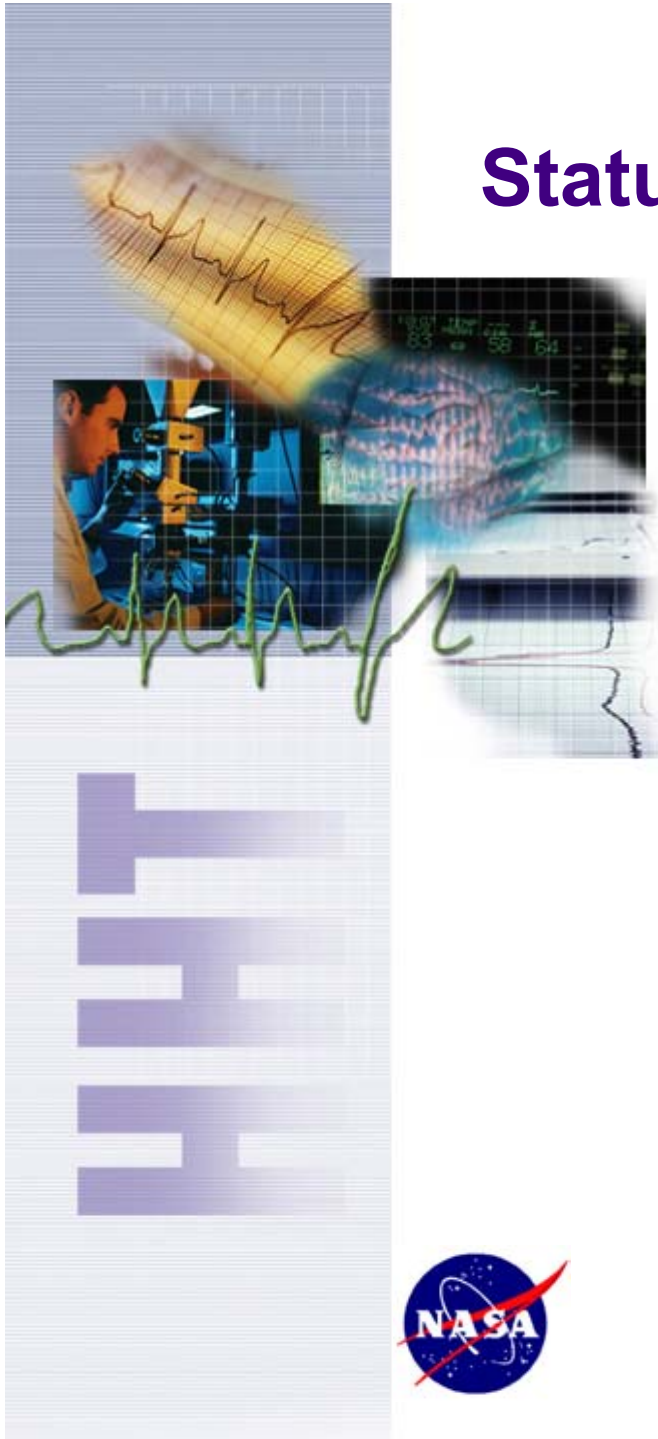
## Drug discovery:

- Assessing protein structure
- Examining protein-protein interactions

## Tissue engineering and design



# Status of Development



- Implemented and tested in the following medical applications:
  - » Blood pressure data from the pulmonary artery of a rat
  - » Pulmonary blood pressure signals in response to step changes in oxygen concentration in the breathing gas
  - » Heart pulse interval comparing sleep apnea condition to a non-apnea condition
  - » Epileptic seizure heart pulse data
- Figures summarizing results can be found in U.S. Patent 6,381,559
- Data and additional results are proprietary and confidential

Status of Development

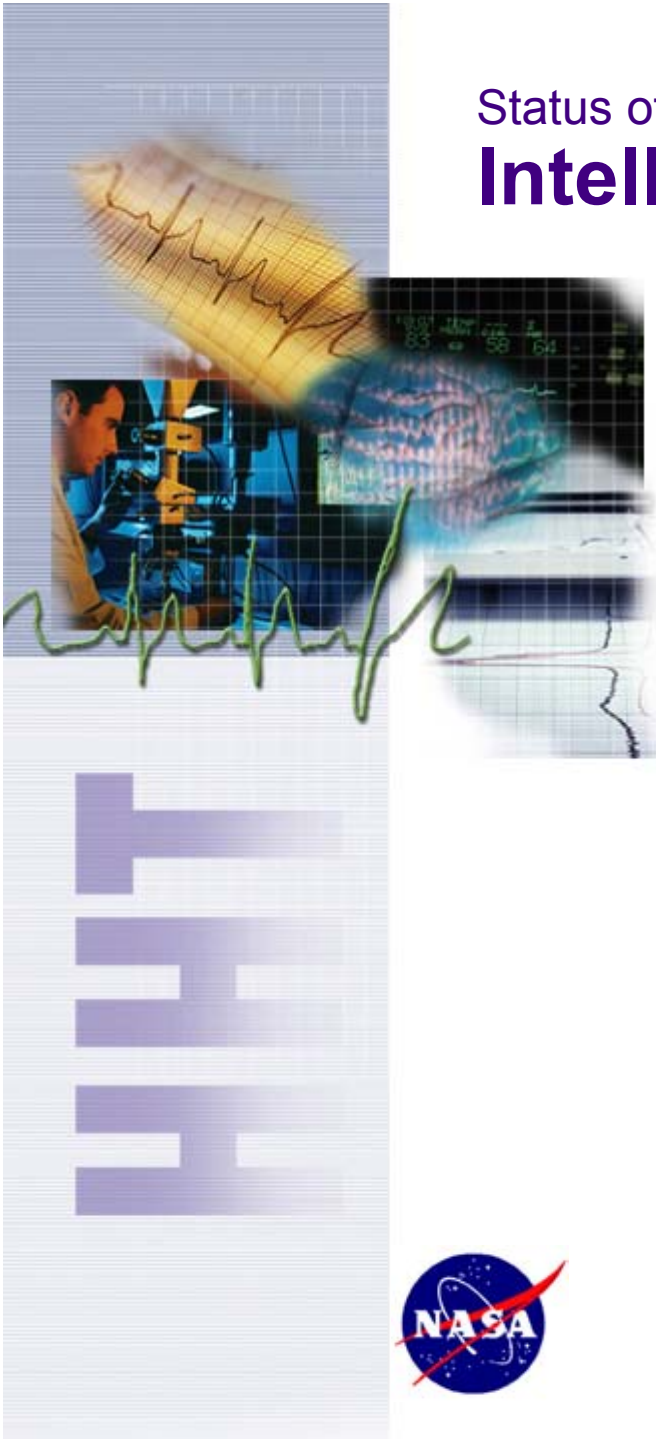
# Intellectual Property Protection

## Issued patents:

- **U.S. Patent No. 6,311,130**  
**Computer Implemented Empirical Mode Decomposition Method, Apparatus, and Article of Manufacture Utilizing Curvature (issued 10/01)**
- **U.S. Patent No. 5,983,162**  
**Computer Implemented Empirical Mode Decomposition Method, Apparatus, and Article of Manufacture (issued 9/99)**

## Copyright:

- **Computer Implemented Empirical Mode Decomposition Method, Apparatus, and Article of Manufacture**



Status of Development

# Intellectual Property Protection

## Pending patents:

- U.S. App. No. 09/082,523  
Extrema Continuation in Part Allowed  
(filed 5/98)
- U.S. App. No. 09/282,424  
Implemented Empirical Mode  
Decomposition Method, Apparatus,  
and Article of Manufacture for  
Analyzing Biological Signals and  
Performing Curve Fitting (filed 3/99)





Status of Development

# Intellectual Property Protection

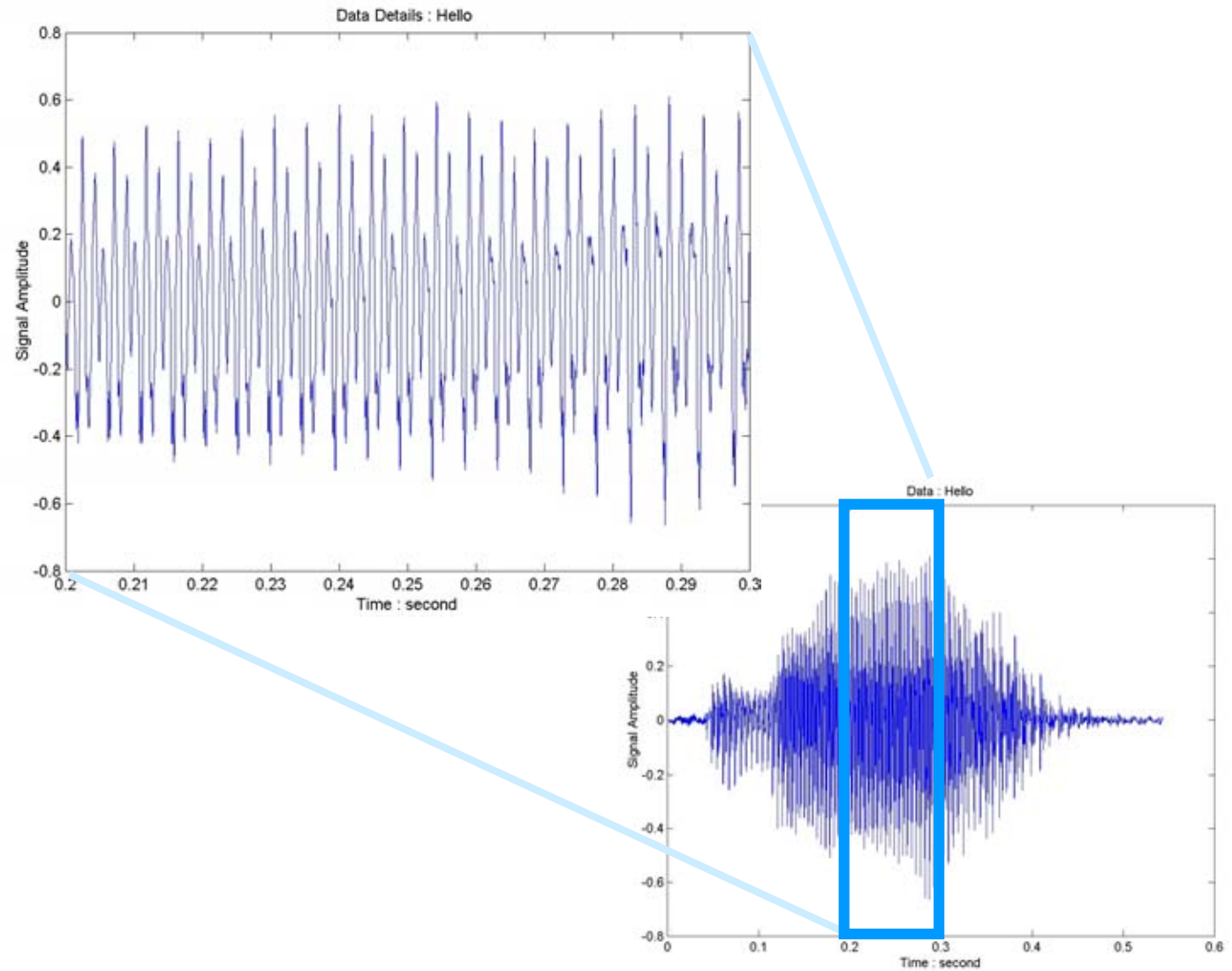
## Pending patents: (cont)

- **U.S. App. No. 09/729,138**  
**Three Dimensional Empirical Mode Decomposition Analysis Apparatus and Method (filed 11/00, inventor Per Gloersen)**
- **U.S. App. No. 10/073,957**  
**Application of HHT for Acoustical Signal Analysis: With Special Emphasis on Speech Analysis, Synthesis, Identification, Enhancement, and Machine Health Monitoring (filed 2/02)**



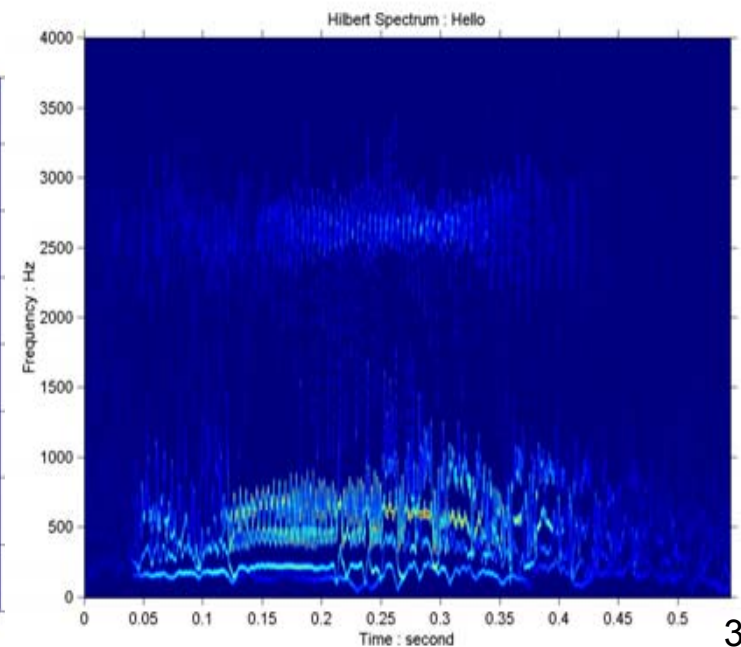
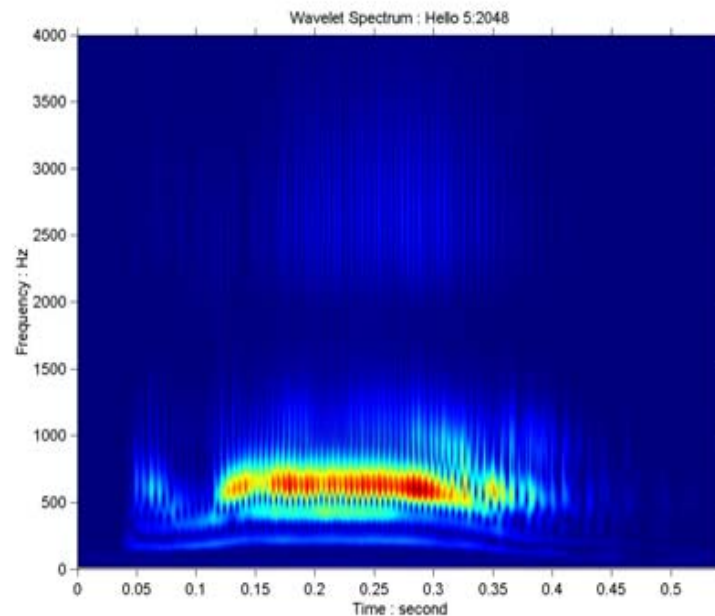
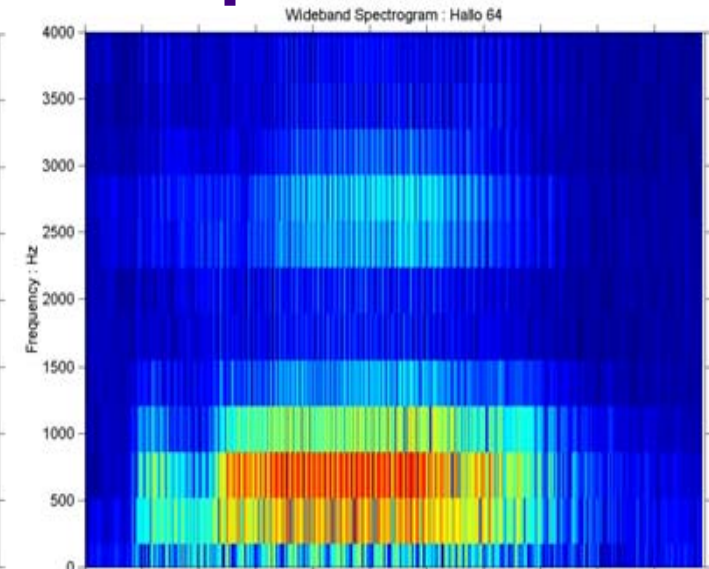
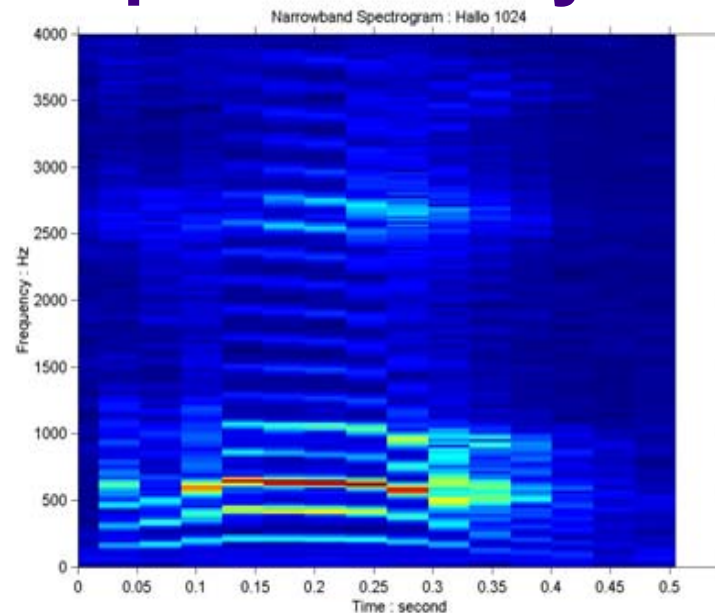
## Technology Details and Results

# Speech Analysis Example

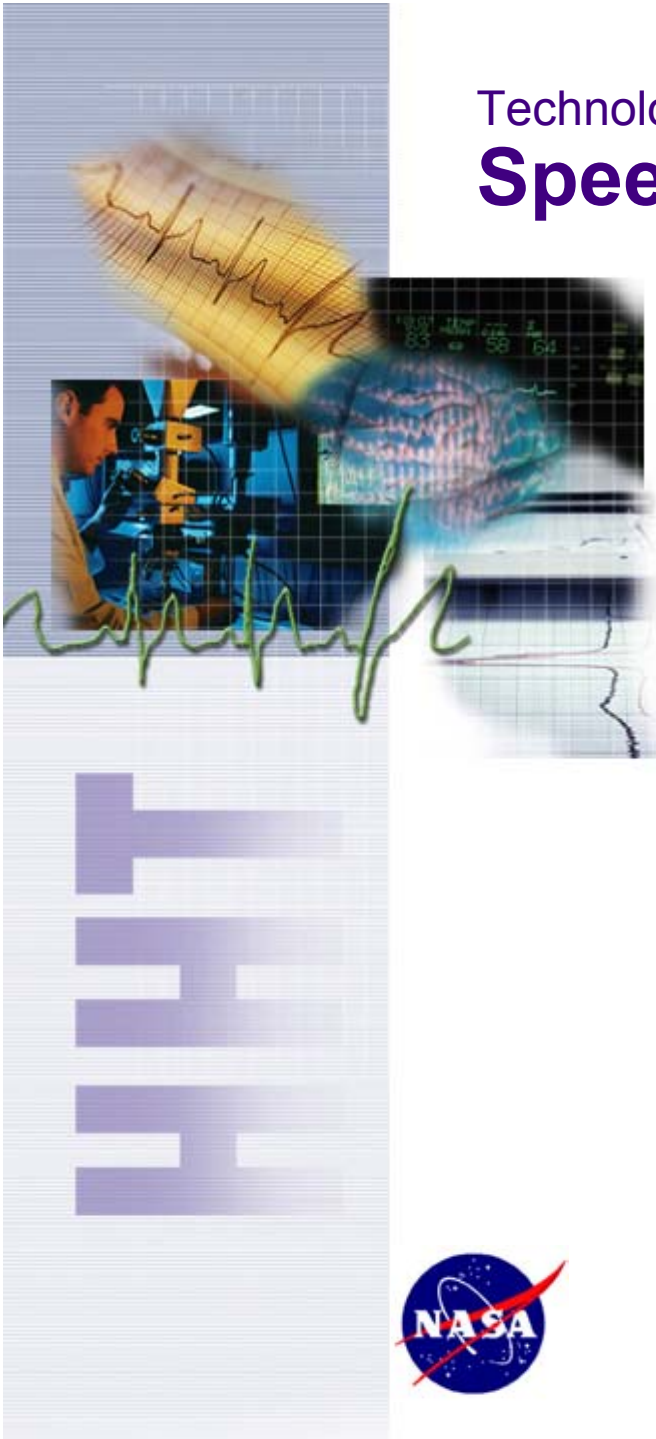


## Technology Details and Results

# Speech Analysis Example



## Speech Analysis Example



### Benefits in sound enhancement:

- **Fourier filter is linear and stationary; it works in frequency domain**
- **Fourier filter takes away harmonics and dulls sharp corners of all fundamentals**
- **EMD filter is nonlinear and intermittent; it works in time domain**
- **EMD filter removes unwanted noise of short periods and leaves fundamentals unchanged**



Technology Details and Results

## Ongoing Work

### Sponsored research, via Space Act Agreements:

- Universities
- Government laboratories

### Conferences:

- SIAM (Society for Industrial and Applied Mathematics) and CAIMS (Canadian Applied and Industrial Mathematics Society) Joint Annual Meeting, 2003; Montreal Canada
- First International Symposium on HHT Developments and Applications, 2003; Taipei, Taiwan





# Summary

- **Licensing and partnering opportunity**
- **Enabling technology with significant commercial potential in medicine**
- **Significant benefits**
  - » **Precision, flexibility, accuracy, easy implementation, real-time operation, and multifunctionality**



# Summary

- Numerous application possibilities
  - » Extracting intrinsic mode functions, aiding in diagnosis, gaining understanding of physiological phenomena
- Intellectual property protected
- Concepts demonstrated in medical applications



## Contact Info

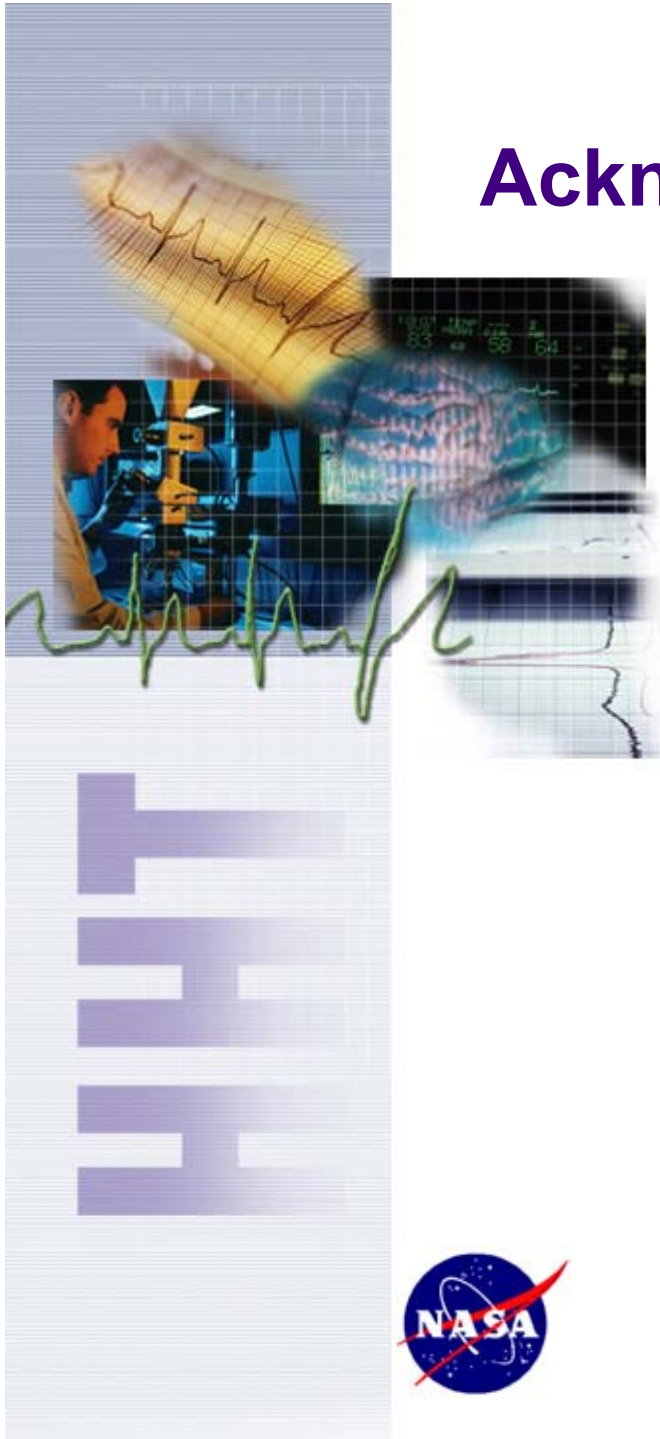
For more information, please contact:

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# Acknowledgements



- **Inventor Norden Huang**
- **Member of National Academy of Engineering**
- **Presentations made at numerous universities and other NASA field centers**
- **Papers published**
  - » **Proceedings of the Royal Society of London**
  - » **Proceedings of the National Academy of Sciences**
  - » **Annual Review of Fluid Mechanics**
  - » **Bulletin of Seismological Society of America**

# Acknowledgements

- **Awards**

- » **NASA Exceptional Space Act, 1998**
- » **Federal Government Technology Leadership Award, 1999**
- » **Federal Laboratory Consortium Technology Development Award, 2001**
- » **R&D 100 Award, 2001**

